MATH 225 Module 3 Lecture e Course Slides (Last Updated: January 7, 2014)

The Complex Plane

There are some ways in which the complex numbers seem like \mathbb{R}^2 .

When we add them, it is done in a component-wise fashion, as we add the real parts together and the imaginary parts together, with neither calculation affecting the others.

And if we multiply a complex number x + yi by a real number s we get sx + syi, which is reminiscent of scalar multiplication.

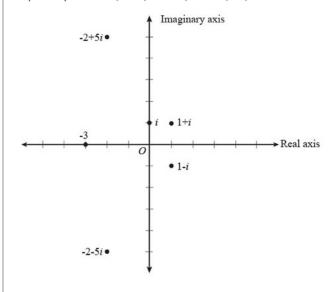
And so it is that when we want to graph complex numbers, we graph them in terms of their two components, the real part and the imaginary part, as though they were elements of \mathbb{R}^2 .

We label the x_1 axis the real axis, and the x_2 axis the imaginary axis, and equate a complex number x + yi with the point (x, y).

The Complex Plane

Example

We plot the points 1 + i, 1 + i, -2 - 5i, -2 - 5i, -3, and i as:



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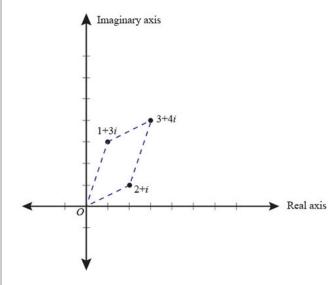
Since complex addition is done componentwise, we still have a parallelogram rule for addition.

And multiplication by a real number also works the same as in \mathbb{R}^2 . But multiplication by a complex number does not have a counterpart in \mathbb{R}^2 .

The Complex Plane

Example

Plot the complex numbers 2 + i, 1 + 3i, (2 + i) + (1 + 3i) = 3 + 4i, 3(2 + i) = 6 + 3i, and (2 + i)(1 + 3i) = -1 + 7i.



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